

Mathematics

Class : X going to XI

1. $(x^2 - 3x + 3)^{x^2 - 16x + 48} = 1$

Case 1: $x^2 - 16x + 48 = 0$

$\Rightarrow x = 12, 4$

Case 2: $x^2 - 3x + 3 = 1$

$\Rightarrow x^2 - 3x + 2 = 0$

$\Rightarrow x = 1, 2$

Case 3: $x^2 - 3x + 3 = -1$ when $x^2 - 16x + 48$ is even

$\Rightarrow x^2 - 3x + 4 = 0$

$D = 9 - 16 = -7 < 0$

\therefore no real solutions

\therefore Product of all real integral solutions = $12 \times 4 \times 2 \times 1 = 96$

Ans. ©

2. $x + y + \frac{5}{x-y} = 10$; $x + y + 2(x - y) = 7$

$\Rightarrow 10 - \frac{5}{x-y} + 2(x-y) = 7$

$\Rightarrow 2a - \frac{5}{a} = -3$ where $x - y = a$

$\Rightarrow 2a^2 + 3a - 5 = 0$

$\Rightarrow 2a^2 - 2a + 5a - 5 = 0$

$\Rightarrow 2a(a - 1) + 5(a - 1) = 0$

$\Rightarrow (a - 1)(2a + 5) = 0$

$\therefore a = 1, a = -\frac{5}{2}$

$\therefore x - y = \frac{-5}{2}$ (not possible)

$\therefore x - y = 1$

$\Rightarrow x + y = 5$

$\therefore 2x = 6$

$$\Rightarrow x = 3, y = 2$$

$$\therefore x^2 + 4y^2 = 9 + 16 = 25$$

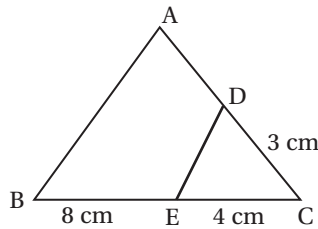
Ans. ©

$$3. \sqrt{\frac{\cot^2 \theta \sec^2 \theta - 1}{\operatorname{cosec}^2 \theta \tan^2 \theta - 1}} + 1 = \sqrt{\frac{\operatorname{cosec}^2 \theta - 1}{\sec^2 \theta - 1}} + 1 = \sqrt{\frac{\cot^2 \theta}{\tan^2 \theta}} + 1$$

$$= \cot^2 \theta + 1 = \operatorname{cosec}^2 \theta$$

Ans. ⑥

4.



$$\frac{EC}{EB} = \frac{CD}{DA}$$

$$\Rightarrow \frac{4}{8} = \frac{3}{DA}$$

$$\therefore DA = 6 \text{ cm}$$

Ans. ①

$$5. \begin{aligned} 153 &= 3^2 \times 17 & \therefore \text{HCF} &= 17 \\ 85 &= 5 \times 17 & \therefore 85x - 153 &= 17 \\ & & \Rightarrow 85x &= 170 \\ & & \therefore x &= 2 \end{aligned}$$

Ans. ⑥

$$6. \begin{aligned} 5 \sec \theta - 2 \tan \theta &= 5 \\ \text{Let } 5 \tan \theta - 2 \sec \theta &= K \\ \therefore (5 \sec \theta - 2 \tan \theta)^2 - (5 \tan \theta - 2 \sec \theta)^2 &= 25 - K^2 \\ \Rightarrow 25(\sec^2 \theta - \tan^2 \theta) + 4(\tan^2 \theta - \sec^2 \theta) &= 25 - K^2 \\ \Rightarrow 25 - 4 &= 25 - K^2 \\ \Rightarrow K^2 &= 4 \Rightarrow K = \pm 2 \\ \therefore 5 \tan \theta - 2 \sec \theta &= 2 \end{aligned}$$

Ans. ①

$$7. \frac{KP}{PE} = \frac{KQ}{QT} \Rightarrow \frac{x-1}{x} = \frac{4x-5}{5x-4}$$

$$\Rightarrow 5x^2 - 5x - 4x + 4 = 4x^2 - 5x$$

$$\Rightarrow x^2 - 4x + 4 = 0 \Rightarrow (x-2)^2 = 0 \Rightarrow x = 2$$

$$\therefore KP = (2-1) \text{ cm} = 1 \text{ cm}, PE = 2 \text{ cm}$$

$$\therefore KE = 3 \text{ cm.}$$

$$\Delta KPQ \sim \Delta KET \Rightarrow \frac{KP}{KE} = \frac{PQ}{ET}$$

$$\Rightarrow \frac{1}{3} = \frac{4 \text{ cm}}{ET} \Rightarrow ET = 12 \text{ cm}$$

$\therefore KI = ET = 12 \text{ cm}$

Ans. (D)

8. Values of a and b can be 2, 3, 5, 7.

$\alpha + \beta = a, \alpha\beta = b \because b$ is prime so one root must be 1.

Let $\alpha = 1 \therefore \beta = b \therefore 1 + b = a$

$\Rightarrow a - b = 1$

$\therefore a = 3, b = 2$

$\therefore a^b = 3^2 = 9$

Ans. (C)

9. $(x^2 - 5)^2 = 16$

$\Rightarrow x^2 - 5 = \pm 4$

$\Rightarrow x^2 = 9$ or $x^2 = 1$

$\Rightarrow x = \pm 3$ or $x = \pm 1$

4 different real values of x .

Ans. (D)

10. $x^3 - ax^2 + bx - 1830$

$\alpha + \beta + \gamma = a, \alpha\beta + \beta\gamma + \alpha\gamma = b, \alpha\beta\gamma = 1830$

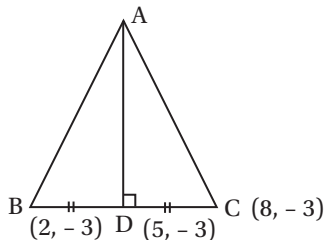
$\Rightarrow \alpha\beta\gamma = 2 \times 3 \times 5 \times 61$

For minimum value of a , three roots will be

6, 5, 61. $a = 6 + 5 + 61 = 72$

Ans. (C)

11.



$AD = \frac{\sqrt{3}}{2} BC = \frac{\sqrt{3}}{2} \times 6 = 3\sqrt{3}$

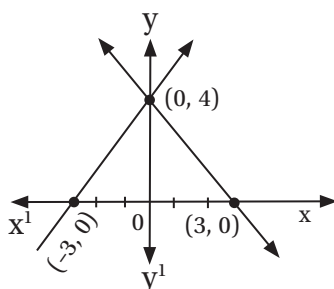
\therefore Co-ordinates of $A(5, 3(\sqrt{3}-1))$

Ans. (B)

12. $4x + 3y = 12, 4x - 3y = -12, y = 0$

For $y = 0, x = 3$ For $y = 0, x = -3$

For $x = 0, y = 4$ For $x = 0, y = 4$



Area = $\frac{1}{2} \times 6 \times 4$

= 12 sq. units

Ans. (B)

13. $\sqrt{a} + \sqrt{b} = 7$

$$2\sqrt{a} + 3\sqrt{b} = 17$$

$$\Rightarrow \sqrt{a} + 2\sqrt{b} = 10$$

$$\frac{-\sqrt{a} \pm \sqrt{b} = 7}{\sqrt{b} = 3 \Rightarrow b = 9}$$

$$\sqrt{b} = 3 \Rightarrow b = 9$$

$$\therefore \sqrt{a} = 4 \Rightarrow a = 16$$

$$\therefore AD^2 = BD \times CD = 16 \times 9 \Rightarrow AD = 12$$

Ans. (A)

14. $\frac{1 + \sin^2 \theta (\cot^2 \theta - 1)}{\cos^2 \theta} = 2^n$

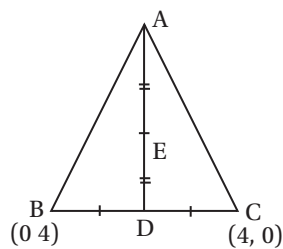
$$\Rightarrow \frac{1 + \sin^2 \theta \cot^2 \theta - \sin^2 \theta}{\cos^2 \theta} = 2^n$$

$$\Rightarrow \frac{\cos^2 \theta + \cos^2 \theta}{\cos^2 \theta} = 2^n$$

$$\Rightarrow 2 = 2^n \Rightarrow n = 1$$

Ans. (A)

15.



$$D = (2, 2)$$

$$\text{Let } A = (x, y)$$

$$\therefore E = \left(\frac{x+2}{2}, \frac{y+2}{2} \right)$$

$$\therefore x = 33, \quad y = 11$$

$$\therefore A(33, 11)$$

Ans. (B)