

# **Monthly Progressive Test (Solution)**

Class: XII

A cademic
Excellence
Programme
TECHNO ACE

**Subject: PCMB** 

# **Physics**

As 
$$E \propto \frac{1}{r}$$

2. A

Q<sub>net</sub> enclosed is zero

3. ©

$$\tau = PE \sin \theta$$

$$4 = (q)(2/100) \times 2 \times 10^5 \times \frac{1}{2}$$

$$2 = q \times 10^3$$

$$q = 2 \text{ mC}$$

4. B

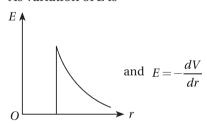
$$A \rightarrow True;$$

$$B \rightarrow True$$

But reason is not the correct explanation of Assertion

5. ©

As variation of E is



6. D

As  $\vdash d - \vdash$ 

As 
$$E = -\frac{dV}{dr}$$

#### 8. D

As 
$$B \propto r$$
  $r \leq R$ 

$$B \propto \frac{1}{r}$$
  $r > R$ 

As 
$$A \bullet \longrightarrow G \longrightarrow R(k\Omega)$$
Voltmeter

$$\frac{1}{2}mv^2 = qv$$

$$r = \frac{mv}{qB} = \frac{m}{qB} \sqrt{\frac{2qv}{m}}$$

$$r \propto \sqrt{v} \implies 2r = \sqrt{4v}$$

# 11. ©

As  $i \propto A \cdot v_d$ 

if  $A(\downarrow)$  then  $v_d(\uparrow)$ 

So, Reason is wrong

#### 12. <sup>©</sup>

Area = 
$$\frac{1}{2} \times 5 \times 5 + 5 \times 5 = 12.5 + 25 = 37.5 \text{ C}$$

## 13. ©

Magnetic field inside paramagnetic is denser.

For diamagnetic it in just opposite.

#### 14. B

$$\begin{split} B = & \frac{\mu_0}{4\pi} \cdot \frac{2M}{r^3} = \frac{\mu_0}{4\pi} (2) \frac{2 \cdot \pi a^2 \cdot 2l(n)i}{r^3} \\ = & \frac{\mu_0}{2} (2) \frac{nla^2}{r^3} \cdot i = \frac{(\mu_0 ni)la^2}{r^3} \end{split}$$

When temperature rises above Curie point ferromagnetic becomes paramagnetic.

#### **16**. **(A**

Magnetic susceptibility of diamagnetic is negative and small.

$$E_0 = WBAN = 60 \times 0.8 \times 0.5 \times 100 = 2400 \text{ Volt}$$

$$i_0 = \frac{2400}{100} = 24 \text{ A}$$

$$E_0 \cdot i_0 = \frac{1}{2} \times 2400 \times 24 = 57600 = 5.76 \times 10^4$$
 watt

18. A

$$v_{avg} = \frac{2v_0}{\pi} = (0.637)v_0$$

19. B

$$M = \frac{L \cdot D}{f_0 \cdot f_e}$$
 where  $D = 25$  cm

20. ©

For telescope 
$$M = \frac{f_0}{f_a}$$

21. B

$$A = r_1 + r_2$$

Condition for minimum deviation  $r_1 = r_2 = r$ 

$$\therefore A = 2r$$

22. ©

$$\beta = \frac{\lambda D}{d} = \lambda \cdot \frac{\left(\frac{D}{3}\right)}{\left(\frac{d}{3}\right)}$$

$$\beta \propto \frac{D}{d}$$

Reason statement is wrong

23. D

All the statements are correct.

24. ®

As stable daughter nucleus.

25. ®

$$E_3 = -\frac{13.6}{3^2} \text{ eV} = -\frac{13.6}{9} \text{ eV} = -1.51 \text{ eV}$$

n = 1 ground state

n = 2 1st excited state

n = 3 second excited state

$$kE = x$$

$$TE = -x$$

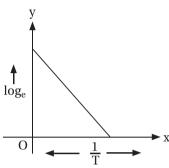
:. 
$$PE = -2x = -3.02 \ eV$$

# Chemistry

26. A

$$K = A.e^{\frac{Ea}{RT}}$$
;

∴  $\log_e K = \log_e A - \frac{Ea}{RT}$ ; Hence graph of  $\log_e K$  vs  $\frac{1}{T}$  will be linear with -ve slope and intercept on y-axis equal to  $\log_e A$ .



27. <sup>(D)</sup>

 $K = A.e^{\frac{-C}{RT}}$ ; Arrhenins equation. The rate constant is inversely related to activation energy. It is energy required to make it equal to threshold level and it can be grater than  $\Delta H$  of the reaction.

28. ©

$$i = 2A$$
,  $t = 5 \times 60 \times 60 S$ 

$$W = 22.2 g$$
;  $A = 177$ 

$$\therefore w = \frac{i \times t \times E}{F} = \frac{i \times t \times \frac{A}{V}}{F}$$

$$\Rightarrow V = \frac{2 \times 5 \times 60 \times 60 \times 177}{22.2 \times 96500} = 3$$

29. B

$$AgCl \rightleftharpoons Ag^+ + Cl^-$$
;  $\Lambda_{sp} = K \Omega^{-1} cm^{-1}$ 

$$\wedge_{sp} = \frac{K \times 1000}{C}$$
;  $\wedge_{AsCl} = \wedge_{Ar}^{o} + \wedge_{Cl}^{o} = x + y$ 

$$(x+y) = \frac{K \times 1000}{C}$$

$$C = \frac{K \times 1000}{(x+y)}$$

$$K_{sp} = C^2 = \left(\frac{K \times 1000}{x + y}\right)^2$$

30. ®

$$CH_3COOH \rightleftharpoons CH_3COO^{\Theta} + H^{\oplus}$$

i > 1, as CH<sub>3</sub>COOH Undergoes ionization in aqueous solution

### 31. ©

0.167 atm; : Na<sub>4</sub>[Fe(CN)<sub>6</sub>] undergoes 60% ionization

$$i = 1 + (n - 1) \alpha = 1 + (5 - 1) \alpha = 1 + 4\alpha$$
  
= 1 + 4(0.6)  
= 3.4

$$C = 2 \times 10^{-3} M$$

$$\pi = i \times CRT$$
= (3.4) (2 × 10<sup>-3</sup>) (0.0823) 300
= 0.167 atm.

#### 32. B

Boiling point decreases as the number of molecules decreases.

#### 33. B

$$b > d > C > a$$

$$b = 0.05 \text{ M glucose}$$
  $n = 0.05$ 

$$d = 0.02 \text{ M KCl} \implies n = 0.04$$

$$C = 0.01 \text{ M } CaCl_2 \Rightarrow n = 0.03$$

$$a = 0.01 \text{ M} \Rightarrow n = 0.02$$

#### 34. ®

has to optically active isomers. Meso is optically inactive

#### 35. ®

Assertion is wrong but reason is correct.

### 36. A

Both assertion and reason are correct and reason is the correct explanation of assertion.

#### 37. A

Both assertion and reason are correct and reason is the correct explanation of assertion.

## 38. ®

Both assertion and reason are correct but reason is not the correct explanation of assertion

#### 39. ©



$$\begin{array}{c|c} & & & \\ \hline & & \\ \hline & \\ \hline & \\ \hline \end{array} \begin{array}{c} \Delta \\ \hline \\ \hline \end{array} \begin{array}{c} + \\ \hline \\ \end{array} \begin{array}{c} + \\ \hline \end{array} \begin{array}{c} + \\ \end{array} \end{array} \begin{array}{c} + \\ \end{array} \begin{array}{c} + \\ \end{array} \begin{array}{c} + \\ \end{array} \end{array} \begin{array}{c} + \\ \end{array} \begin{array}{c} + \\ \end{array} \begin{array}{c} + \\ \end{array} \begin{array}{c} + \\ \end{array} \end{array} \begin{array}{c} + \\ \end{array} \begin{array}{c} + \\ \end{array} \end{array} \begin{array}{c} + \\ \end{array} \begin{array}{c} + \\ \end{array} \begin{array}{c} + \\ \end{array} \end{array} \begin{array}{c} + \\ \end{array} \begin{array}{c} + \\ \end{array} \end{array} \begin{array}{c} + \\ \end{array} \begin{array}{c} + \\ \end{array} \end{array} \begin{array}{c}$$

41. ®

III > I > II

→ Decreasing acidic order

42. ©

OCH<sub>3</sub> OH 
$$+$$
 CH<sub>3</sub>J (Anisole)

43. ®

$$\alpha$$
-H is present  $\frac{1}{O}$   $OH^{(-)}$   $OH^{(-)}$ 

44. ®

$$\begin{array}{c|c}
O & & O \\
\hline
H_2(gas, 1atm) & \\
\hline
Pd/carboethanol & \\
\end{array}$$

45. A

$$C = CH$$

$$HO - C = CH_2$$

$$HgSO_4$$

$$H_2SO_4$$

$$(enol)$$

$$(keto)$$

$$Acetophenon$$

46. ©

Glucose does not react with NaHSO<sub>3</sub>

47. ®

Fructose reduces Tollen's reagent due to enolisation of fructose followed by conversion to aldehyde by base.

During mutarotation of  $\beta$ -D-glucose in aqueous solution angle of optical rotation changes from an angle of +19.2° to a constant value of +52.5°.

49. ®

[Pt(Py)(NH<sub>3</sub>)(Br)(Cl)] will have three geometrical isomers.

- 50. A
  - (a) XeF<sub>2</sub> Linear
  - (b) XeF<sub>4</sub> Square planar
  - (c) XeO<sub>3</sub> Pyramidal
  - (d) XeOF<sub>4</sub> Square pyramidal

# **Mathematics**

51. ®

 $R = \{(1, 2), (1, 3), (1, 4)\}$  is not symmetric  $R = \{(1, 2), (2, 1)\}$  is symmetric but not reflexive and not transitive.

52. ©

$$f(x) = x^2 + 12$$

$$f(x_1) = f(x_2)$$

$$\Rightarrow$$
 x<sub>1</sub><sup>2</sup> + 12 = x<sub>2</sub><sup>2</sup> + 12

$$\Rightarrow$$
  $x_{12} = x_{22}$ 

$$\Rightarrow$$
 x<sub>1</sub> = x<sub>2</sub>

$$(:: x \in N)$$

 $\Rightarrow$  f(x) is one - one (injective) function.

Codomain= N

but range is subset of N.

- $\therefore$  f(x) is not onto function.
- $\therefore$  f(x) is injective.
- 53. ©

$$sin^{-1} (sin6)$$
=  $sin^{-1} \{ sin (2\pi + 6 - 2\pi) \}$ 
=  $sin^{-1} \{ sin (6 - 2\pi) \}$ 
=  $6 - 2\pi$ 

54. ©

$$5\cos^{-1}\left(\frac{1}{2}\right) + 7\sin^{-1}\left(\frac{-1}{2}\right)$$

$$= 5\cos^{-1}\left(\cos\frac{\pi}{3}\right) + 7\sin^{-1}\left\{\sin\left(\frac{-\pi}{6}\right)\right\}$$

$$= \frac{5\pi}{3} + 7\left(\frac{-\pi}{6}\right)$$

$$= \frac{5\pi}{3} - \frac{7\pi}{6} = \frac{10\pi - 7\pi}{6} = \frac{3\pi}{6} = \frac{\pi}{2}$$

$$\begin{bmatrix} 2+x & 3 & 4 \\ 1 & -1 & 2 \\ x & 1 & -5 \end{bmatrix}$$
 is a singular matrix.

$$\begin{vmatrix} 2+x & 3 & 4 \\ 1 & -1 & 2 \\ x & 1 & -5 \end{vmatrix} = 0$$

$$\Rightarrow$$
 (2 + x) (5 - 2) - 3 (-5 - 2x) + 4 (1 + x) = 0

$$\Rightarrow$$
 6 + 3x + 15 + 6x + 4 + 4x = 0

$$\Rightarrow 13x + 25 = 0$$

$$\Rightarrow$$
 x =  $\frac{-25}{13}$ 

56. ®

A is a square matrix of order 3.

$$|A| = -4$$

$$|Adj A| = |A|^{n-1} = |A|^2 = (-4)^2 = 16$$

57. ©

$$\frac{\mathrm{d}}{\mathrm{dx}} \log(\log x^5)$$

$$\frac{d}{dx}\log(\log x^5)$$

$$= \frac{1}{\log x^5} \times \frac{d}{dx}(\log x^5)$$

$$= \frac{1}{\log x^5} \times \frac{5}{x}$$

$$=\frac{5}{x\log x^5}$$

58. ®

$$x = 6 \sin^{-1}(2t), y = \frac{1}{\sqrt{1 - 4t^2}}$$

$$\frac{dx}{dt} = \frac{6}{\sqrt{1 - 4t^2}} \times 2 \qquad \frac{dy}{dt} = -\frac{1}{2} (1 - 4t^2)^{\frac{-3}{2}} \times -8t$$

$$\frac{12}{\sqrt{1-4t^2}}$$

$$= \frac{12}{\sqrt{1-4t^2}} = \frac{4t}{(1-4t^2)\sqrt{1-4t^2}}$$

$$\therefore \frac{dy}{dx} = \frac{\cancel{A}t}{(1-4t^2)\sqrt{1-4t^2}} \times \frac{\sqrt{1-4t^2}}{\cancel{12}}$$

$$=\frac{t}{3(1-4t^2)}$$

$$f(x) = \frac{\sin x^{2}}{x}, x \neq 0$$

$$= 0, x = 0$$

$$\lim_{x \to 0} f(x)$$

$$= \lim_{x \to 0} \frac{\sin x^{2}}{x}$$

$$= \lim_{x \to 0} \frac{\sin x^{2}}{x^{2}} \times x = 1 \times 0 = 0$$

$$f(0) = 0$$

$$f(0) = \lim_{x \to 0} f(x)$$

$$f(x) = \lim_{x \to 0} f(x)$$

$$\therefore$$
 f(x) is continuous at x = 0.

$$Rf'(0) = \lim_{h \to 0} \frac{f(o+h) - f(o)}{h}$$

$$= \lim_{h \to 0} \frac{\frac{\sin h^2}{h} - 0}{h} = 1$$

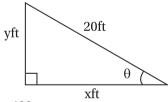
$$= \lim_{h \to 0} \frac{\sin h^2}{h^2} = 1$$

Lf'(0) = lim  

$$h \to 0$$
  $\frac{f(o-h) - f(o)}{-h}$   
= lim  
 $h \to 0$   $\frac{\sin h^2}{h^2} = 1$ 

$$\therefore Rf'(0) = Lf'(0)$$

$$\therefore$$
 f(x) is derivable at x = 0



$$\therefore x^2 + y^2 = 400$$

When 
$$x = 12$$
,  $y^2 = 400 - 144 = 256$ 

$$\therefore y = 16$$

$$\frac{dy}{dt} = -2ft/sec.$$

$$x^2 + y^2 = 400$$

$$\Rightarrow 2x \frac{dx}{dt} + 2y \frac{dy}{dt} = 0$$

$$\Rightarrow x\frac{dx}{dt} + y\frac{dy}{dt} = 0$$

$$\Rightarrow 12\frac{\mathrm{dx}}{\mathrm{dt}} + 16(-2) = 0$$

$$\Rightarrow \frac{dx}{dt} = \frac{3\cancel{2}^8}{\cancel{12}_3} = \frac{8}{3} \text{ ft/sec.}$$

Let 
$$m = \tan \theta = \frac{y}{x}$$

$$\therefore \frac{dm}{dt} = \frac{d}{dt} \left( \frac{y}{x} \right) = \frac{x \frac{dy}{dt} - y \frac{dx}{dt}}{x^2}$$

$$= \frac{12(-2) - 16 \times \frac{8}{3}}{144}$$

$$= \frac{-200^{25}}{3 \times 144_{18}} = \frac{-25}{54}$$

$$f'(x) = 2x^3 + 3x^2 - 36x + 10$$

$$f'(x) = 6x^2 + 6x - 36$$

$$f'(x) = 0 \Rightarrow 6x^{2} + 6x - 36 = 0$$
$$\Rightarrow x^{2} + x - 6 = 0$$
$$\Rightarrow x = -3, 2$$

$$f''(x) = 12x + 6$$

at 
$$x = -3$$
,  $f''(-3) = -36 + 6 = -30 < 0$ 

$$\therefore$$
 f(x) is maximum at x = -3.

at 
$$x = 2$$
,  $f''(2) = 12 \times 2 + 6 = 30 > 0$ .

$$\therefore$$
 f(x) is minimum at x = 2.

∴ Point of minimum is 2.

#### 62. D

$$\int_{1}^{2} x^{2} \log x \, dx$$

$$= \left[ \log x \times \frac{x^{3}}{3} \right]_{1}^{2} - \int_{1}^{2} \frac{1}{x} \times \frac{x^{3}}{3} \, dx$$

$$= \frac{8}{3} \log 2 - \frac{1}{3} \int_{1}^{2} \frac{1}{x} \times \frac{x^{3}}{3} \, dx$$

$$= \frac{8}{3} \log 2 - \frac{1}{3} \left[ \frac{x^{3}}{3} \right]_{1}^{2}$$

$$= \frac{8}{3} \log 2 - \frac{1}{9} [8 - 1]$$

$$= \frac{8}{3} \log 2 - \frac{7}{9}$$

$$\int 2x^3 e^{x^2} dx$$

$$= \int 2x \times x^2 e^{x^2} dx \qquad \text{Let } x^2 = t$$

$$= \int t e^t dt \qquad \therefore 2x dx = dt$$

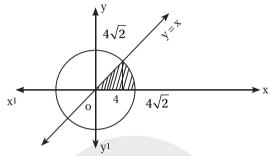
$$= t e^t - e^t + C$$

$$= e^t (t-1) + C$$

$$= e^{x^2} (x^2 - 1) + C$$



$$x = 4$$



Area = 
$$\int_{0}^{4} x \, dx + \int_{4}^{4\sqrt{2}} \sqrt{32 - x^{2} \, dx}$$

$$= \left[\frac{x^2}{2}\right]_0^4 + \left[\frac{x\sqrt{32 - x^2}}{2} + \frac{32}{2}\sin^{-1}\left(\frac{x}{4\sqrt{2}}\right)\right]_4^{4\sqrt{2}}$$

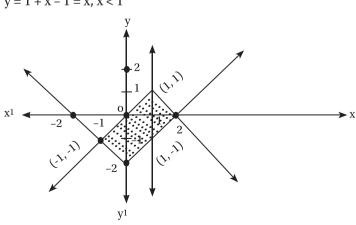
$$= 8 + 16 \times \frac{\pi}{2} - (8 + 16 \times \frac{\pi}{4})$$

$$= 8 + 8\pi - 8 - 4\pi$$

=  $4\pi$  sq. units.

65. A

$$\begin{array}{ll} y = |x|-2 \;, & y = 1-|x-1| \\ y = x-2, \, x \geq 0 & y = 1-x+1, \, x \geq 1 \\ y = -x-2, \, x < 0 & = 2-x, \, x \geq 1 \\ y = 1+x-1 = x, \, x < 1 \end{array}$$



Area = 
$$\int_{0}^{1} x \, dx + \int_{1}^{2} (2-x) \, dx + \left| \int_{0}^{2} (x-2) dx \right| + \left| \int_{-1}^{0} y \, dy \right| + \left| \int_{-2}^{-1} (-y-2) dy \right|$$
  
=  $\left[ \frac{x^{2}}{2} \right]_{0}^{1} + \left[ 2x - \frac{x^{2}}{2} \right]_{1}^{2} + \left| \frac{x^{2}}{2} - 2x \right|_{0}^{2} + \left| \frac{y^{2}}{2} \right|_{-1}^{0} + \left| \frac{-y^{2}}{2} - 2y \right|_{-2}^{-1}$   
=  $\frac{1}{2} + \frac{1}{2} + 2 + \frac{1}{2} + \frac{1}{2} = 4$  sq. units

$$\vec{r} = \lambda(\hat{i} + 2\hat{j} - \hat{k})$$

 $\therefore$  equation of line is  $\frac{x}{1} = \frac{y}{2} = \frac{z}{-1}$ 

67. (a) 
$$\vec{r} = \lambda(\hat{i} + 2\hat{j} - \hat{k})$$
  
 $\vec{r} = 3\hat{i} + 3\hat{j} + \mu)2\hat{i} + \hat{j} + \hat{k}$ 

$$\vec{a}_{1} = \vec{0}, \vec{a}_{2} = 3\hat{i} + 3\hat{j}, \vec{b}_{1} = \hat{i} + 2\hat{j} - \hat{k}, \vec{b}_{2} = 2\hat{i} + \hat{j} + \hat{k}$$

$$\vec{a}_{2} - \vec{a}_{1} = 3\hat{i} + 3\hat{j}, \vec{b}_{1} \times \vec{b}_{2} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & -1 \\ 2 & 1 & 1 \end{vmatrix} = 3\hat{i} - 3\hat{j} - 3\hat{k}$$

$$\therefore \left| \vec{\mathbf{b}}_1 \times \vec{\mathbf{b}}_2 \right| = \sqrt{9 + 9 + 9} = 3\sqrt{3}$$

$$(\vec{a}_2 - \vec{a}_1).(\vec{b}_1 \times \vec{b}_2) = 9 - 9 + 0 = 0$$

 $\therefore$  S. D. = 0 unit.

68. ©

Since S. D. of two lines is zero.

$$\vec{r} = \lambda(\hat{i} + 2\hat{j} - \hat{k})$$
 and  $\vec{r} = 3\hat{i} + 3\hat{j} + \mu(2\hat{i} + \hat{j} + \hat{k})$  are intersecting lines.

Any point on the first line be (t, 2t, -t)

:. 
$$t\hat{i} + 2t\hat{j} - t\hat{k} = (3 + 2\mu)\hat{i} + (3 + \mu)\hat{j} + \mu\hat{k}$$

$$\Rightarrow$$
 3 + 2  $\mu$  = t

$$3 + \mu = 2t$$

$$\mu = -t$$

$$\therefore$$
 3 = 3t  $\Rightarrow$  t = 1

 $\therefore$  Point of intersection is (1, 2, -1)

 $\therefore$  The motorcyles will meet with an accident at (1, 2, -1).

69. A

$$P(E) = \frac{13}{52} = \frac{1}{4}, P(F) = \frac{1}{13}$$

$$P(E \cap F) = \frac{1}{52}$$

$$\therefore P(E/F) = \frac{\frac{1}{52}}{\frac{1}{13}} = \frac{1}{4} = P(E) \text{ and } P(F/E) = \frac{\frac{1}{52}}{\frac{1}{4}} = \frac{1}{13} = P(F)$$

Again, 
$$P(E \cap F) = \frac{1}{4} \times \frac{1}{13} = P(E) \times P(F)$$

:. Assertion is true. Reason is also true and reason is the correct explanation of assertion (A).

70. ®

If A and B be two independent events.

$$\therefore P(A \cap B) = P(A)P(B)$$

Assertion (A) is false. But reason is correct.

71. ©

$$\frac{d^{3}y}{dx^{3}} - 3 \left(\frac{d^{2}y}{dx^{2}}\right) + 2 \left(\frac{dy}{dx}\right)^{4} + y^{3} = 0$$

 $\therefore$  Order = 3, degree = 1.

72. <sup>(D)</sup>

$$\frac{dy}{dx} + 8x = 16x^{2} + 4$$

$$\Rightarrow dy = (16x^{2} + 4 - 8x) dx$$

$$\Rightarrow \int dy = \int 16x^{2} dx + 4 \int dx - 8 \int x dx$$

$$\Rightarrow y=16 \times \frac{x^3}{3} + 4x - 8 \times \frac{x^2}{2} + c$$
$$\Rightarrow y = \frac{16}{3}x^3 + 4x - 4x^2 + c$$

When x = 1, y = 
$$\frac{1}{3}$$
  
 $\frac{1}{3} = \frac{16}{3} + 4 - 4 + 6$ 

$$\frac{1}{3} = \frac{16}{3} + 4 - 4 + c$$

$$\therefore y = \frac{16}{3}x^3 + 4x - 4x^2 - 5$$

73. B

$$Max Z = 5x + 10y$$

Subject to 
$$x + 2y \le 120$$

$$x + y \ge 60$$

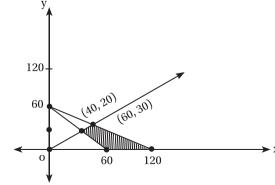
$$x - 2y \ge 0$$

$$x \ge 0$$
,  $y \ge 0$ 

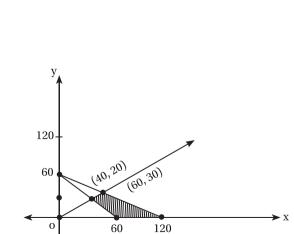
For 
$$x + 2y = 120$$

For 
$$x + y = 60$$

For 
$$x = 2y$$



Corner points one (40, 20), (60, 30), (120, 0) and (60, 0).



at 
$$(40, 20)$$
,  $Z = 200 + 200 = 400$ 

at 
$$(120, 0)$$
,  $Z = 300 + 300 = 600$ 

at 
$$(120, 0)$$
,  $Z = 600$ 

at 
$$(60, 0)$$
,  $Z = 300$ 

Max. value of Z = 600.

74. ©

$$Min Z = 6x + 21y$$

Subject to 
$$x + 2y \ge 3$$

$$x + 4y \ge 4$$

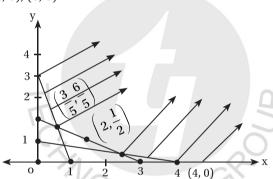
$$3x + y \ge 3$$

$$x \ge 0$$
,  $y \ge 0$ 

For 
$$x + 2y = 3$$
,  $(3, 0)$ ,  $(1, 1)$ 

For 
$$x + 4y = 4$$
,  $(4, 0)$ ,  $(0, 1)$ 

For 
$$3x + y = 3$$
,  $(1, 0)$ ,  $(0, 3)$ 



Corner points of the unbounded region are (0, 3),  $\left(\frac{3}{5}, \frac{6}{5}\right)$ ,  $\left(2, \frac{1}{2}\right)$  and (4, 0).

at 
$$(0, 3)$$
,  $Z = 63$ 

at 
$$\left(\frac{3}{5}, \frac{6}{5}\right)$$
,  $Z = \frac{18}{5} + \frac{126}{5} = \frac{144}{5} = 28.8$ 

at 
$$\left(2, \frac{1}{2}\right)$$
,  $Z = 12 + \frac{21}{2} = \frac{45}{2} = 22.5$ 

at 
$$(4, 0)$$
,  $Z = 24$ 

Now, 6x + 21y < 22.5 determines the open half plane where no point is common with the feasible region.

Min Z = 22.5 at 
$$(2, \frac{1}{2})$$
.

75. ©

$$= \int \frac{\mathrm{dx}}{\cos^3 x \sqrt{2\sin 2x}}$$

$$= \int \frac{dx}{\cos^3 x \sqrt{2 \sin 2x}}$$

$$= \int \frac{dx}{\cos^3 x \sqrt{2 \times 2 \sin x \cos x}}$$

$$= \int \frac{dx}{\cos^4 x \sqrt{\tan x}}$$

$$= \int \frac{\mathrm{dx}}{\cos^4 x \sqrt{\tan x}}$$

$$= \frac{1}{2} \int \frac{\sec^2 x \times \sec^2 x \, dx}{\sqrt{\tan x}} \qquad \text{Let } \tan x = z^2$$

$$= \frac{1}{2} \int \frac{(1+z^4) \, 2 \, \cancel{z} \, dz}{\cancel{z}}$$

$$= \int dz + \int z^4 dZ$$

$$= z + \frac{z^5}{5} + k$$

$$= (\tan x)^{\frac{1}{2}} + \frac{(\tan x)^{\frac{5}{2}}}{5} + k$$

$$\therefore (\tan x)^{\frac{1}{2}} + \frac{1}{5} (\tan x)^{\frac{5}{2}} + k = (\tan k)^A + C(\tan x)^B + k$$

$$\Rightarrow A = \frac{1}{2}, C = \frac{1}{5}, B = \frac{5}{2}$$

$$\therefore A + B + C = \frac{1}{2} + \frac{5}{2} + \frac{1}{5} = \frac{16}{5}$$

# **Biology**

76. ®

Lie close to each other

77. A

12.

78. ®

1.

79. ®

The marsupials are examples of divergent evolution.

The Australian mammals are examples of convergent evolution. In convergent evolution, organisms not closely related, independently evolve similar traits as a result of adaptation to similar environment or ecological niches.

80. A

Morphine.

81. ©

*Trichoderma polysporum*-Statin Statin is obtained from *Monascus purpureas* 

82. A

By elution

83. **(A**)

PCR.

The DNA polymerase obtained from the microbe , can be heated to a temperature high enough to melt DNA and yet is still able to function.

84. A Formation of hydrogen bonds between sticky ends of DNA fragments. 85. ® Commensalism. 86. A Both A and R are true and R is the correct explanation of A. 87. B Both A and R are true but R is not the correct explanation of A. 88. A Both A and R are true and R is the correct explanation of A. 89. © A is true but R is false. The amphibians evolved into reptiles. 90. B Both A and R are true but R is not the correct explanation of A 91. A Diploid; mitosis. 92. A Spermiation. 93. A One second polar body and one ovum. 94. A Secretory phase. 95. © This occurs due to failure of segregation of chromatids during cell division cycle, resulting in the gain of chromosomes. 96. A A polypeptide of 24 amino acids will be formed. UAA is a termination codon which will stop the polypeptide synthesis. So the resultant polypeptide will have 24 amino acids. 97. © Klinefelter's syndrome. 98. ® The diversity in the organisms living in the region.

100. A

Cynodon.

99. B

Lesser inter-specific competition.